

## COURSE OUTLINE

### (1) GENERAL

<b>SCHOOL</b>	SCIENCE		
<b>ACADEMIC UNIT</b>	DEPARTMENT OF MATHEMATICS		
<b>LEVEL OF STUDIES</b>	POSTGRADUATE <b>Studies in Mathematics</b>		
<b>COURSE CODE</b>	<b>313-1106</b>	<b>SEMESTER</b>	<b>A</b>
<b>COURSE TITLE</b>	MEASURE THEORY		
<b>INDEPENDENT TEACHING ACTIVITIES</b> <i>if credits are awarded for separate components of the course, e.g. lectures, laboratory exercises, etc. If the credits are awarded for the whole of the course, give the weekly teaching hours and the total credits</i>	<b>WEEKLY TEACHING HOURS</b>	<b>CREDITS</b>	
	3	10	
<i>Add rows if necessary. The organisation of teaching and the teaching methods used are described in detail at (d).</i>			
<b>COURSE TYPE</b> <i>general background, special background, specialised general knowledge, skills development</i>	SPECIALISED GENERAL KNOWLEDGE		
<b>PREREQUISITE COURSES:</b>	NO		
<b>LANGUAGE OF INSTRUCTION and EXAMINATIONS:</b>	GREEK		
<b>IS THE COURSE OFFERED TO ERASMUS STUDENTS</b>	YES		
<b>COURSE WEBSITE (URL)</b>	<a href="http://www.samos.aegean.gr/samos_math/pms/lessonseng.php">http://www.samos.aegean.gr/samos_math/pms/lessonseng.php</a>		

### (2) LEARNING OUTCOMES

<p><b>Learning outcomes</b></p> <p><i>The course learning outcomes, specific knowledge, skills and competences of an appropriate level, which the students will acquire with the successful completion of the course are described.</i></p> <p>Consult Appendix A</p> <ul style="list-style-type: none"> <li>● <i>Description of the level of learning outcomes for each qualifications cycle, according to the Qualifications Framework of the European Higher Education Area</i></li> <li>● <i>Descriptors for Levels 6, 7 &amp; 8 of the European Qualifications Framework for Lifelong Learning and Appendix B</i></li> <li>● <i>Guidelines for writing Learning Outcomes</i></li> </ul>		
<p>Mastering the material described in the syllabus (see (3) below)</p>		
<p><b>General Competences</b></p> <p><i>Taking into consideration the general competences that the degree-holder must acquire (as these appear in the Diploma Supplement and appear below), at which of the following does the course aim?</i></p> <table style="width: 100%; border: none;"> <tr> <td style="width: 50%; vertical-align: top;"> <i>Search for, analysis and synthesis of data and information, with the use of the necessary technology</i>  <i>Adapting to new situations</i>  <i>Decision-making</i>  <i>Working independently</i>  <i>Team work</i>  <i>Working in an international environment</i>  <i>Working in an interdisciplinary environment</i>  <i>Production of new research ideas</i> </td> <td style="width: 50%; vertical-align: top;"> <i>Project planning and management</i>  <i>Respect for difference and multiculturalism</i>  <i>Respect for the natural environment</i>  <i>Showing social, professional and ethical responsibility and sensitivity to gender issues</i>  <i>Criticism and self-criticism</i>  <i>Production of free, creative and inductive thinking</i>            .....  <i>Others...</i>            .....         </td> </tr> </table>	<i>Search for, analysis and synthesis of data and information, with the use of the necessary technology</i> <i>Adapting to new situations</i> <i>Decision-making</i> <i>Working independently</i> <i>Team work</i> <i>Working in an international environment</i> <i>Working in an interdisciplinary environment</i> <i>Production of new research ideas</i>	<i>Project planning and management</i> <i>Respect for difference and multiculturalism</i> <i>Respect for the natural environment</i> <i>Showing social, professional and ethical responsibility and sensitivity to gender issues</i> <i>Criticism and self-criticism</i> <i>Production of free, creative and inductive thinking</i> ..... <i>Others...</i> .....
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<p>Working independently</p>		

Working in an interdisciplinary environment  
Production of free, creative and inductive thinking

### (3) SYLLABUS

Algebras and  $\sigma$ -algebras of sets. Measurable and non measurable sets.  
Outer measure and Lebesgue measure. Mesurable spaces and Measure spaces.  
Measurable functions. Measurability and limit. Measure transformations.  
Markov, Chebyshev and Holder inequalities.  
Limit and integral: Fatou's Lemma, Monotone Convergence Theorem and Lebesgue Dominated Convergence Theorem.  
Product space and product measure, Fubini's Theorem. Integration by parts.  
 $L_p$  spaces and their basic properties. The Hilbert space  $L_2$ .  
Signed measures and Hahn decomposition. Absolute continuity and singularity.  
The Radon-Nikodym Theorem.  
Borel Measures on locally compact Hausdorff spaces. Bounded linear functionals on the space of continuous functions and Riesz Representation Theorem.

### (4) TEACHING and LEARNING METHODS - EVALUATION

<p style="text-align: center;"><b>DELIVERY</b> <i>Face-to-face, Distance learning, etc.</i></p>	Face-to-face	
<p style="text-align: center;"><b>USE OF INFORMATION AND COMMUNICATIONS TECHNOLOGY</b> <i>Use of ICT in teaching, laboratory education, communication with students</i></p>	Communication with students via e-mail	
<p style="text-align: center;"><b>TEACHING METHODS</b> <i>The manner and methods of teaching are described in detail. Lectures, seminars, laboratory practice, fieldwork, study and analysis of bibliography, tutorials, placements, clinical practice, art workshop, interactive teaching, educational visits, project, essay writing, artistic creativity, etc.</i></p> <p><i>The student's study hours for each learning activity are given as well as the hours of non-directed study according to the principles of the ECTS</i></p>	<b>Activity</b>	<b>Semester workload</b>
	Lectures	39
	Independent study	148.5
	Assignments	62.5
	Course total (25 per ECTS)	<b>250</b>
<p style="text-align: center;"><b>STUDENT PERFORMANCE EVALUATION</b> <i>Description of the evaluation procedure</i></p> <p><i>Language of evaluation, methods of evaluation, summative or conclusive, multiple choice questionnaires, short-answer questions, open-ended questions, problem solving, written work, essay/report, oral examination, public presentation, laboratory work, clinical examination of patient, art interpretation, other</i></p> <p><i>Specifically-defined evaluation criteria are given, and if and where they are accessible to students.</i></p>	<p>Student evaluation is done in Greek through a written examination which includes short-answer equations and problem solving.</p> <p>For students with disabilities, evaluation takes place via oral exams.</p>	

## **(5) ATTACHED BIBLIOGRAPHY**

*- Suggested bibliography:*

1. Real Analysis, M. Anoussis, A. Tsolomitis, V. Felouzis, Symmetria publishers, 2014 (in Greek).
2. Measure and Integral, R.L. Wheeden & A. Zygmund, Chapman & Hall/CRC Pure and Applied Mathematics
3. Real Analysis: Modern techniques and their applications, G. Folland, 2<sup>nd</sup> Edition, Wiley & Sons, Inc. 1999.
4. Read Analysis, H.L. Royden, Macmillan publishing company, 1988.